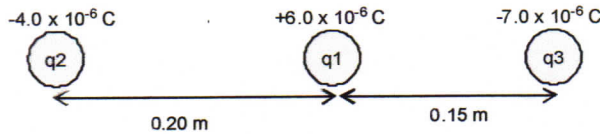


Name: Key

Review Worksheet

Electric Forces and Fields

1. The figure below shows three point charges that lie along the x axis.



- a. Determine the magnitude and direction of the net electrostatic force on charge  $q_1$ :

$$F_{E_{q2}} = \frac{k(-4\mu C)(6\mu C)}{(0.2m)^2} = -5.4 N \quad \text{left}$$

$$F_{E_{q3}} = \frac{k(6\mu C)(-7\mu C)}{(0.15m)^2} = -16.8 N \quad \text{Right}$$

$$16.8 - 5.4 = 11.4 N \quad \text{to the right}$$

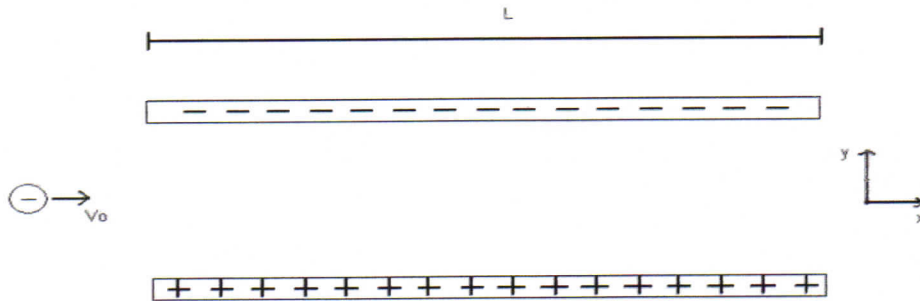
- b. Determine the magnitude and direction of the electric field at the point where  $q_1$  lies:

$$E = \frac{kQ_2}{r^2} = 900,000 N/C$$

$$E = \frac{kQ_3}{r^2} = 2800000 N/C$$

$$E_{\text{total}} = 1,900,000 N/C \quad \text{to the right}$$

2. An electron enters the region of a uniform electric field as shown below. Assume the initial velocity of the particle to be  $3.0 \times 10^6$  m/s and the Electric Field strength to be 200 N/C. The horizontal length of the plates is also known to be 10.0 cm.



- a. Find the acceleration of the electron while in the field:

$$ma = F_e \quad ma = QE$$

$$a = \frac{QE}{m}$$

$$a = -3.51 \times 10^{13} m/s^2$$

- b. Find the time at which it leaves the field if it enters at  $t = 0s$ :

Constant velocity in x-direction

$$.1m = (3 \times 10^6 m/s)(t)$$

$$t = 3.3 \times 10^{-8} s$$

- c. What is its vertical position when it leaves the field if it enters at  $y_0 = 0m$ ?

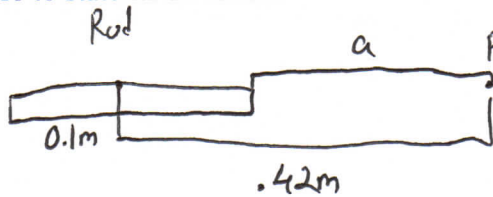
$$\Delta y = \frac{1}{2}at^2 + v_{0y}t$$

$$\Delta y = \frac{1}{2}(-3.51 \times 10^{13})(3.7 \times 10^{-8})^2$$

$$\Delta y = -0.02m \quad \text{or} \quad 2cm$$

3. A rod 10.0 cm long is uniformly charged and has a total charge of  $-25.0 \mu\text{C}$ . Determine the magnitude and direction of the electric field along the axis of the rod at a point 42.0 cm from its center. Make sure to state its direction.

$\square$  N/C



$$L = .1\text{m}$$

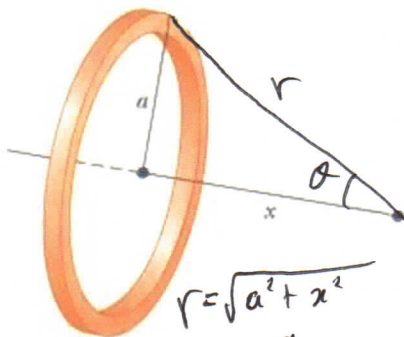
$$a = .42 - .05 = 0.37\text{m}$$

$$E = \frac{kQ}{a(L+a)} = 1.29 \times 10^6 \text{ N/C}$$

we proved this earlier

towards rod

4. Below is a uniformly charged ring of total charge  $Q$  and radius  $a$ . Determine an expression for the electric field strength along the axis of the ring at a distance  $x$  from the center of the ring.



$$r = \sqrt{a^2 + x^2}$$

$$\cos\theta = \frac{x}{\sqrt{a^2 + x^2}}$$

$$dE_x = \frac{k dq}{r^2} \cos\theta - \text{only want } x \text{ direction. } y \text{ cancels out.}$$

$$= \frac{k da}{a^2 + x^2} \cdot \frac{x}{\sqrt{a^2 + x^2}}$$

$$= \frac{k x da}{(a^2 + x^2)^{3/2}}$$

$$= \frac{k x}{(a^2 + x^2)^{3/2}} \int dq$$

$$E = \frac{k x Q}{(a^2 + x^2)^{3/2}}$$

5. Find the electric field on the axis of the ring from #4 at the following distances from the center of the ring. Assume that  $a = 10.0 \text{ cm}$  and the ring has a total charge of  $93.0 \mu\text{C}$ .

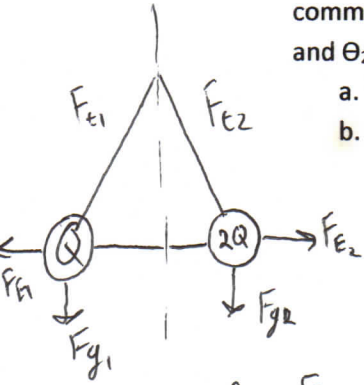
a.  $\frac{1.00 \text{ cm}}{8.24} \text{ i MN/C}$

b.  $\frac{5.00 \text{ cm}}{29.9} \text{ i MN/C}$

c.  $\frac{30.00 \text{ cm}}{7.93} \text{ i MN/C}$

Use equation from problem #4

6. Two small spheres of mass  $m$  are suspended from string of length  $l$  that are connected at a common point. One sphere has charge  $Q$  and the other charge  $2Q$ . The strings make angles  $\theta_1$  and  $\theta_2$  with the vertical.



$x - F_{E1} = F_{t1} \sin \theta$      $F_{E2} = F_{t2} \sin \theta$   
 $y - F_{t1} \cos \theta = F_{g1}$      $F_{t2} \cos \theta = F_{g2}$   
 For small  $\theta$   $H$  and  $L$  are almost the same.  
 so we know that  $\sin \theta = \tan \theta = \theta$

- a. Explain how  $\theta_1$  and  $\theta_2$  are related - they are the same bc  $\theta$  is very small  
 b. Assume  $\theta_1$  and  $\theta_2$  are small. Show that the distance between the spheres is approximately

$$r \approx \left( \frac{4k_e Q^2 l}{mg} \right)^{1/3}$$

$$F_{E1} = F_{t1} \sin \theta$$

$$F_{E1} = F_{t1} \sin \theta$$

$$F_{E1} = \frac{mg}{\cos \theta} = mg \tan \theta$$

$$\frac{2kQ^2}{r^2} = mg \frac{r}{2L}$$

$$r = \left( \frac{4kQ^2 l}{mg} \right)^{1/3}$$

7. A charged cork ball of mass 1.00g is suspended on a light string in the presence of a uniform electric field. When  $E = (3.00i + 5.00j) \times 10^5 \text{ N/C}$ , the ball is in equilibrium at  $\theta = 37^\circ$ . Find:

- a. The charge on the ball  
 b. The tension in the string

$$T_x = F_{Ex} = Eq = (3 \times 10^5)(Q)$$

$$T \sin \theta = (3 \times 10^5)(Q)$$

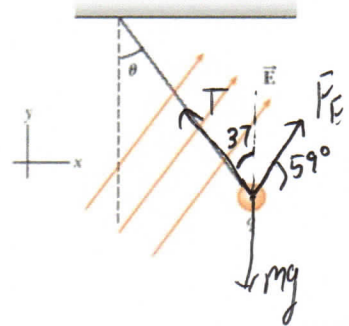
$$T = 4.98 \times 10^5 Q$$

$$(0.001 \text{ kg})(9.8) = T \cos(37) + (5 \times 10^5)(Q)$$

$$Q = 1.09 \times 10^{-8} \text{ C}$$

$$T = (4.98 \times 10^5)(1.09 \times 10^{-8})$$

$$T = 0.0054 \text{ N}$$



$$T_x = F_{Ex}$$

$$mg = T_y + F_{Ey}$$