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U5: Homework Questions \#1

## Rotational Kinematics and Moment of Inertia

1. A bar on a hinge starts from rest and rotates with an angular acceleration $\alpha=(14+5 t)$ $\mathrm{rad} / \mathrm{s}^{2}$, where $t$ is in seconds. Determine the angle in radians through which the bar turns in the first 4.09 s .
```
174
rad
```

2. A centrifuge in a medical laboratory rotates at an angular speed of $3450 \mathrm{rev} / \mathrm{min}$. When switched off, it rotates 48.0 times before coming to rest. Find the constant angular acceleration of the centrifuge.
3. A rotating wheel requires 3.03 s to rotate through 37.0 revolutions. Its angular speed at the end of the 3.03 s interval is $97.9 \mathrm{rad} / \mathrm{s}$. What is the constant angular acceleration of the wheel?
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14
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$\mathrm{rad} / \mathrm{s}^{2}$
4. In the figure to the right: $m=1.8 \mathrm{~kg}$ and $M=3.3 \mathrm{~kg}$.

(a) Calculate the moment of inertia of the array of point objects shown above about the vertical axis.

(b) Calculate the moment of inertia of the array of point objects shown above about the horizontal axis.

5. A rigid rod of length $L$ and mass $M$ rotates about its center of mass ( $z$ axis in picture). Prove that the moment of inertia for the rod is:

$$
I=(1 / 12) M L^{2}
$$


6. A solid cylinder rotates about an axis that lies directly through its center. Prove that the moment of inertia of this cylinder $I$ is equal to:

$$
I=1 / 2 M R^{2}
$$

*A Hint:

> *With the bar examples, we looked at the ratio $\mathrm{dm} / \mathrm{dr}$. Here, think about starting with a ratio of $\mathrm{dm} / \mathrm{dV}$ and trying to get it back to dr .

- " V " is volume

